## High School Algebra Playlist: Relating the Domain of a Function to its Graph

Aligns with CCSS.Math.Content.HSF.IF.B.5: Relate the domain of a function to its graph and, where applicable, to the quantitative relationship it describes. For example, if the function $h(n)$ gives the number of person-hours it takes to assemble $n$ engines in a factory, then the positive integers would be an appropriate domain for the function

## Related Standards

- CCSS.Math.Content.HSF.IF.A.1: Understand that a function from one set (called the domain) to another set (called the range) assigns to each element of the domain exactly one element of the range. If $f$ is a function and $x$ is an element of its domain, then $f(x)$ denotes the output of $f$ corresponding to the input $x$. The graph of $f$ is the graph of the equation $y=f(x)$.
- CCSS.Math.Content.HSF.IF.B.4: For a function that models a relationship between two quantities, interpret key features of graphs and tables in terms of the quantities, and sketch graphs showing key features given a verbal description of the relationship. Key features include: intercepts; intervals where the function is increasing, decreasing, positive, or negative; relative maximums and minimums; symmetries; end behavior; and periodicity.


## Objectives

In this module, you will learn and practice the following skills:

- relate the domain of a function to its graph
- understand the appropriate domain for a function modeling a situation


## Let's get started!

## Key Terms

- A function is a relation which has each input related to exactly one output.
- The domain of a function is the set of input values.
- The range of a function is the set of output values.


## Connections

- https://openstaxcollege.org/textbooks/algebra-and-trigonometry; section 3.2


## Relating the Domain of a Function to its Graph

## (CCSS.Math.Content.HSF.IF.B.5)

A function is a relation which has each input related to exactly one output. The domain of a function is the set of input values. The range of a function is the set of output values.

If your students...

## Mishandle restrictions on the domain of a function:

A typical problem is to think of the domain of a function as "all reals" when the function is actually restricted to non-negative values or to integers. Remind students that they can't count a quarter of a person.

WATCH: Evaluate mathematical situations by analyzing the domain and range of functions
https://learnzillion.com/lesson plans/4659\#fndtn-lesson

## Confuse domain and range:

Students think of "range" in its common English usage as meaning a variety of values, so they often get domain and range confused. Remind them that these pairs are each in alphabetic order:

Domain, $x$, horizontal, input
Range, $y$, vertical, output
Assume a function is continuous and misidentify the range:
Many functions that appear to be continuous really are step functions. If a boat-rental place advertises its prices as " $\$ 10$, plus $\$ 3$ per hour or portion thereof", then the graph of time vs. price is not a straight line - it is a step function. So the range of the function is not all non-negative reals but $13,16,19,22$, etc.

