



Kinematics

2 Dimensional Motion

Projectile Example Problem

Name _____

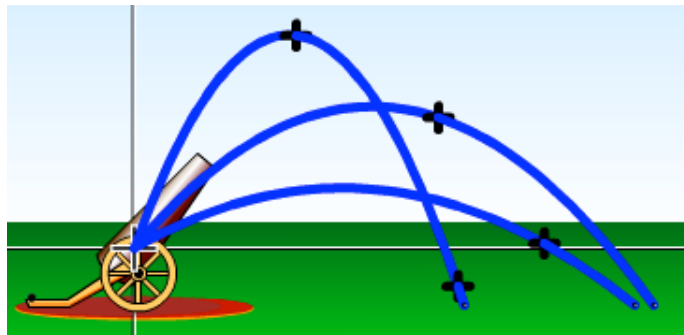
Teacher _____

Period _____

Purpose – To investigate projectiles fired at angles.

An object is fired at a speed of 14 m/s at three different angles.

- Identify the trajectories in the chart below on the diagram to the right as v_1 , v_2 or v_3 .
- Resolve each of the velocity vectors into horizontal and vertical components.
- Rank the time of flight for each velocity.



Velocity	Horizontal Component	Vertical Component	Time of Flight
$v_1 = 14 \text{ m/s at } 30^\circ$			
$v_2 = 14 \text{ m/s at } 50^\circ$			
$v_3 = 14 \text{ m/s at } 70^\circ$			

Launch the Projectile Motion simulation. <http://phet.colorado.edu/en/simulation/projectile-motion>

Adjust the speed to 14 m/s then fire three projectiles at 30° , 50° and 70° . Keep all other initial conditions as given.

Draw an FBD for each of the three shots and circle one of the three choices, \uparrow \downarrow zero, that describes the projectile's motion. Ignore air resistance.

v_1 while ascending

● v: \uparrow \downarrow zero
 a: \uparrow \downarrow zero
 ΣF : \uparrow \downarrow zero

v_2 at the apex

● v: \uparrow \downarrow zero
 a: \uparrow \downarrow zero
 ΣF : \uparrow \downarrow zero

v_3 while descending

● v: \uparrow \downarrow zero
 a: \uparrow \downarrow zero
 ΣF : \uparrow \downarrow zero

Circle either constant, changing or zero, draw an arrow in the direction of the velocity and give the value of the acceleration of the projectile while in the air. Ignore air resistance.

While the projectile is ascending its:

- horizontal velocity is constant/changing/zero and points _____ and the acceleration is _____
- vertical velocity is constant/changing/zero and points _____ and the acceleration is _____

When the projectile is at the apex its:

- horizontal velocity is constant/changing/zero and points _____ and the acceleration is _____
- vertical velocity is constant/changing/zero and points _____ and the acceleration is _____

While the projectile is descending its:

- horizontal velocity is constant/changing/zero and points _____ and the acceleration is _____
- vertical velocity is constant/changing/zero and points _____ and the acceleration is _____

In the chart to the right, identify each of the following equations as describing either horizontal or vertical motion.

List the two different types of motion.
 _____, _____

Which type of motion describes the horizontal equation(s) _____

Which type of motion describes the vertical equation(s) _____

Equation	Horizontal Motion	Vertical Motion
$v = \frac{\Delta d}{\Delta t}$		
$a = \frac{v_f - v_i}{\Delta t}$		
$\Delta d = v_i \Delta t + \frac{1}{2} a \Delta t^2$		
$a = \frac{v_f^2 - v_i^2}{2 \Delta d}$		

What ties the horizontal and vertical equations of motion together? _____

Rewrite the equations below adding the subscripts "x" and "y" to the appropriate variables. Where appropriate replace the acceleration "a" with "g".

		Projectile Motion Equation	
Equation		Horizontal (X)	Vertical (Y)
$v = \frac{\Delta d}{\Delta t}$	becomes		
$a = \frac{v_f - v_i}{\Delta t}$	becomes		
$\Delta d = v_i \Delta t + \frac{1}{2} a \Delta t^2$	becomes		
$a = \frac{v_f^2 - v_i^2}{2 \Delta d}$	becomes		

Adjust the cannon's position until the crosshair on the cannon lies on the horizon (ground level). Fire a projectile at 14 m/s at 40° above the horizontal. Calculate the time of flight, the range and the maximum height of the projectile. Use the tape measure to check your answers. All measurements will be made with the tape measure in the horizontal or vertical position.



Time of Flight

Range

Height

time = 1.84 seconds

Left click on the cannon and hold. Adjust the vertical elevation of the cannon. Fire another projectile at 14 m/s at 40° above the horizontal. How does the vertical elevation affect the time of flight, the range and height of the projectile?